Inappropriate meaning:

Definitions from Oxford Languages

• Not suitable or proper in the circumstances *"there are penalties for inappropriate behaviour"*

Derogatory meaning:

Definitions from Oxford Languages

• Showing a critical or disrespectful attitude "she tells me I'm fat and is always making derogatory remarks"

Defamatory meaning:

Definitions from Oxford Languages

 (of remarks, writing, etc.) damaging the good reputation of someone; slanderous or libellous.
"a defamatory allegation"